## REPORT DOCUMENTATION PAGE

Form Approved OMB NO. 0704-0188

Public Reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comment regarding this burden estimates or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188,) Washington, DC 20503.

1. AGENCY USE ONLY (Leave Blank)

2. REPORT DATE
April 2001

3. REPORT TYPE AND DATES COVERED
Final progress, 7/1/96-6/6/007

Final progress, 7/1/96-9/8/00
301000

4. TITLE AND SUBTITLE

A Fast PDE Solver Environment for Large-Scale Applications

Department of Mathematics, University of South Carolina, LeConte

DAAHO4-96-1-0326

6. AUTHOR(S)

Bjorn Jawerth

8. PERFORMING ORGANIZATION REPORT NUMBER

13060-F195

5. FUNDING NUMBERS

9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES)

7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)

U. S. Army Research Office P.O. Box 12211

College, Columbia, SC 29208

Research Triangle Park, NC 27709-2211

10. SPONSORING / MONITORING AGENCY REPORT NUMBER

ARO Grant # DAAH04-96-1-036

36197.1-RT-DPS

11. SUPPLEMENTARY NOTES

The views, opinions and/or findings contained in this report are those of the author(s) and should not be construed as an official Department of the Army position, policy or decision, unless so designated by other documentation.

12 a. DISTRIBUTION / AVAILABILITY STATEMENT

12 b. DISTRIBUTION CODE

Approved for public release; distribution unlimited.

13. ABSTRACT (Maximum 200 words)

The major achievements of this project have been summarized in the Interim Progress Reports. The results of most significance fall in the following major categories. Quasilinear PDEs, the Eikonal Equation, and the Image Irradiance Equation; Photometric Stereo and Interactive Visual Design; Discrete Curvature; Lattice Boltzmann Simulation of Discrete Curvature Flow by Mean Curvature for computer vision and image processing; and Electromagnetic Scattering from Non-Smooth Domains and new Piecewise Polynomial Wavelet Bases

20010607 036

14. SUBJECT TERMS			15. NUMBER OF PAGES
Eikonal equation, disc	6 pages incl. this one		
Lattice-Boltzmann, Inte	16. PRICE CODE		
17. SECURITY CLASSIFICATION	18. SECURITY CLASSIFICATION	19. SECURITY CLASSIFICATION	20. LIMITATION OF ABSTRACT
OR REPORT	ON THIS PAGE	OF ABSTRACT	
UNCLASSIFIED	UNCLASSIFIED	UNCLASSIFIED	l UL



Office of Sponsored Programs and Research  $May\ 11,\ 2001$ 

Army Research Office ATTN: David Seitz 4300 South Miami Boulevard Durham, NC 27703-9142

RE: ARO Grant # DAAH04-96-1-036

Dear Mr. Seitz:

Enclosed please find the following reports for the subject award:

Interim Progress Reports for Years 1 through 4 (one of each) Final Progress Report Reports on Inventions and Subcontracts

Thank you for your patience in allowing the University to work out obtaining these reports from Dr. Jawerth. If you have any questions or need any additional information, please call me at (803) 777-7093 or contact me via e-mail at <u>path@spar.sc.edu</u>.

Sincerely,

Patricia F. Hatcher

Sponsored Program Administrator

admicea F Hatcher

Enclosures

cc:

R. Stephenson

T. Huggins

UNIVERSITY OF SOUTH CAROLINA BICENTENNIAL 1801-2001

MASTER COPY: PLEASE KEEP THIS "MEMORANDUM OF TRANSMITTAL" BLANK FOR REPRODUCTION PURPOSES. WHEN REPORTS ARE GENERATED UNDER THE ARO SPONSORSHIP, FORWARD A COMPLETED COPY OF THIS FORM WITH EACH REPORT SHIPMENT TO THE ARO. THIS WILL ASSURE PROPER IDENTIFICATION. NOT TO BE USED FOR INTERIM PROGRESS REPORTS; SEE PAGE 2 FOR INTERIM PROGRESS REPORT INSTRUCTIONS.

#### **MEMORANDUM OF TRANSMITTAL**

U.S. Army Research Office ATTN: AMSRL-RO-BI (TR) P.O. Box 12211 Research Triangle Park, NC 27709-2211	MAY 1 5 2001		
Reprint (Orig + 2 copies)	Technical Report (Orig + 2 copies)		
Manuscript (1 copy)	X Final Progress Report (Orig + 2 copies)		
	Related Materials, Abstracts, Theses (1 copy)		
CONTRACT/GRANT NUMBER: AF	RO Grant # DAAH04-96-1-036		
REPORT TITLE: A FAST PDE SOL	VER ENVIRONMENT FOR LARGE-SCALE APPLICATIONS		
is forwarded for your information.			
SUBMITTED FOR PUBLICATION TO (applicable only if report is manuscript):			

Sincerely,

Björn Jawerth

# REPORT DOCUMENTATION PAGE (SF298) (Continuation Sheet)

1. List of Manuscripts: See separate pages.

# 2. Scientific Personnel supported and Honors/Awards/Degrees:

Patrik Andersson

Alexander Andrianov

Colin Bennett

Emil Comea

Fredrik Ekstedt

Fausto Espinal

Stephen Fenner

Michael Hilton

Ralph Howard

Terry Huntsberger

Björn Jawerth

Göran Kronquist

Toshiro Kubota

Martin Lindberg

Yiping Mao

Per Gunnar Martinsson

Johan Råde

Henrik Storm

Sundaram V.

Weimin Zheng

- 3. Report of Inventions: --
- 4. Scientific Progress and Accomplishments: See separate pages.
- 5. Technology transfer: --

# A FAST PDE SOLVER ENVIRONMENT FOR LARGE-SCALE APPLICATIONS

#### **FINAL PROGRESS REPORT**

Björn Jawerth

**April 28, 2001** 

U.S. ARMY RESEARCH OFFICE

ARO Grant # DAAH04-96-1-036

Department of Mathematics University of South Carolina Columbia, SC 29208

APPROVED FOR PUBLIC RELEASE DISTRIBUTION UNLIMITED

THE VIEWS, AND/OR FINDINGS CONTAINED IN THIS REPORT ARE THOSE OF THE AUTHOR(S) AND SHOULD NOT BE CONSTRUED AS AN OFFICIAL DEPARTMENT OF THE ARMY POSITION, POLICY, OR DECISION, UNLESS SO DEIGNATED BY OTHER DOCUMENTATION

Program directors: Dr. Anna Tsao and Dr. Dennis Healy (DARPA)

### A. STATEMENT OF PROBLEM STUDIED

The objective of this project is to solve Partial Differential Equations associated with descriptions of three-dimensional objects and interactive visual design for manufacturing, design and simulation, and to investigate corresponding computer vision and image processing problems.

#### **B. SUMMARY OF THE MOST IMPORTANT RESULTS**

The major achievements of this project have been summarized in the Interim Progress Reports. The results of most significance fall in the following major categories.

- Quasilinear PDEs, the Eikonal Equation, and the Image Irradiance Equation.
- Photometric Stereo and Interactive Visual Design
- Discrete Curvature
- Lattice Boltzmann Simulation of Flow by Mean Curvature for computer vision and image processing
- Electromagnetic Scattering from Non-Smooth Domains and new Piecewise Polynomial Wavelet Bases

For the Eikonal Equation and related first-order nonlinear equations we have obtained a detailed understanding of solutions near singular points. The main results are that there is a strong lack of uniqueness of solutions near such points and that solutions can be less regular than both the function H and the initial data of the problem, but that this loss of regularity only occurs along a pair of curves through the singular point.

For photometric stereo we have focused on reducing the number of photometric images required and on improving the surface integration from the normals. A novel method for surface integration has been developed. It is different then traditional methods, in that it lets the geometry drive the integration path. This method divides the surface into small regions. The surface is integrated over each small path.

The Four Vertex Theorem is a classical theorem involving the extreme points of Euclidean curvature. This theorem was extended by B. Dahlberg (see Interim Progress report Year 1) to cover simple polygons and the appropriate notion of discrete Euclidean curvature. We have generalized this to the affine setting. The correct statement involves a new (discrete) affine curvature. We obtain a discrete six-vertex theorem (generalizing the well-known, classical and nondiscrete setting).

We have studied lattice Boltzmann models for advanced image processing algorithms. The principal advantage of the lattice Boltzmann method over traditional techniques for obtaining solutions of PDEs is that they are naturally well suited for fully parallel machines, resulting in very fast codes. Below we describe several different applications of the lattice Boltzmann model to sonar and image processing.

In recent years nonlinear diffusion has become a powerful tool for intra-region smoothing of images. The results of nonlinear diffusion can be used to obtain an enhanced image or as a precursor to higher-level processing such as image segmentation, shape description, and object detection and tracking. We have developed a lattice Boltzmann model for image filtering by a reaction-diffusion equation. We have tested our methods on various kinds of noisy images including infrared airborne radar images and sonar images. The results are promising.

We have developed a lattice Boltzmann model for mean curvature motion. We have overcome the difficulty of finding a proper collision operator in the lattice Boltzmann equation by using the diffusion generated motion by mean curvature approach.

Based on diffusion generated motion, we have developed a shape recovery system. Our system is capable of recovering shapes of multiple objects, and it automatically changes topology as it searches for the object boundary.

The boundary value problem for the time-harmonic Maxwell equations for a domain in 3D or 2D, can be reduced to solving a layer potential integral equation on the boundary (a surface in 3D or a curve in 2D) of the domain. To study the solutions of these types of equations, we have developed a new class of piecewise polynomial wavelet bases.

#### C. LIST OF PUBLICATIONS AND TECHNICAL REPORTS

- 1] E. Cornea, R. Howard, and P-G Martinsson, "The Eikonal and Related First Order Non-linear Partial Differential Equations in Two Independent Variables," preprint.
- [2] L. Andersson, R. Howard, and G. Galloway, "A Strong Maximum Principle for Weak Solutions of Quasi-Linear Elliptic Equations with Applications to Lorentzian Geometry", preprint.
- [3] L. Andersson, R. Howard, and G. Galloway, "Regularity Properties of the Cosmological Time Function"
- [4] L. Andersson and R. Howard, "Rigidity Results for Robertson-Walker Spacetimes"
- [5] E.D. Sinzinger and B. Jawerth, "Surface representation from photometric stereo with wavelets", in Proc. SPIE Conf. on Wavelet Applications, Vol. 3169, San Diego, CA, 1997.
- [6] B. Jawerth and Y. Mao, "Interactive Visual Design of Surfaces", preprint.
- [7] M. L. Hilton and R. T. Ogden. "Data analytic threshold selection in 2D signal de-noising," to appear in *IEEE Transactions on Signal Processing*.
- [8] Y. Mao, "Multiresolution analysis and general sampling lattices", preprint.
- [9] T. Kubota and T. L. Huntsberger, "Edge dipole and edge field for boundary detection," in *Proc. SPIE Conf. Hybrid Image and Signal Processing VI*, Vol. 3389, Orlando, FL, Apr 1998.
- [10] F. Espinal and R. Chandran, "Wavelet-based fractal signature for texture classification," in *Proc. SPIE Conf. on Wavelet Applications V*, Vol. 3391, Orlando, FL, Apr 1998.
- [11] T. Kubota and T. L. Huntsberger, "Adaptive pattern recognition system for scene segmentation," *Optical Engineering, Special Section on Advances in Pattern Recognition*, Vol. 37, No. 3, pp. 829-835, 1998.
- [12] F. Espinal, T. L. Huntsberger, B. Jawerth, and T. Kubota, "Wavelet-based fractal signature analysis for automatic target recognition," *Optical Engineering, Special Section on Advances in Pattern Recognition*, Vol. 37, No. 1, pp. 166-174, 1998.

- [13] G. Fernandez and T. L. Huntsberger, "Wavelet-based system for recognition and labeling of polyhedral junctions," *Optical Engineering, Special Section on Advances in Pattern Recognition*, Vol. 37, No. 1, pp. 158-165, 1998.
- [14] T. Kubota, T. L. Huntsberger and C. O. Alford, "A vision system with real-time feature extractor and relaxation network," to appear in *Int. Journal Pattern Recognition and Artificial Intelligence*, May 1998.
- [15] T. L. Huntsberger and J. Rose, "Computer Simulation of Bimodal Neurons and Networks: Integrating Infrared and Visual Stimuli," chapter in <u>Computer Simulation of Complex Biological Systems</u>, (Ed. I. S. Iyengar), CRC Press, 1998.
- [16] T. L. Huntsberger, "Autonomous multirover system for complex planetary retrieval operations," in *Proc. SPIE Symposium on Sensor Fusion and Decentralized Control in Autonomous Robotic Agents*, Vol. 2905, Pittsburgh, PA, Oct 1997, pp. 11-17.
- [17] B. Jawerth, P. Lin, and E.D. Sinzinger, "Lattice Boltzmann methods for anisotropic diffusion of images", *Mathematical Imaging*, in review.
- [18] K. Debure and T. Kubota, "Autoregressive Texture Segmentation and Synthesis for Wavelet Image On Compression", 10th Image and Multidimensional Digital Signal Processing Workshop, July 1998, Austria.
- [19] S. Godavarthy and T. L. Huntsberger, "Global illumination using Overlapping Wavelets", *Proc.* 8th International Conference on Engineering Computer Graphics and Descriptive Geometry (ICECGDG), Aug 1998, Austin, TX.
- [20] E.D. Sinzinger, "Numerical Methods for Ill-Posed Problems in Image Processing and Computer Vision", M.S. Thesis, Department of Computer Science, University of South Carolina, Columbia, SC, 1998.
- [21] M. Lindberg, "A new general class of piecewise polynomial wavelet bases", preprint.
- [22] B. Jawerth, P. Lin, and E.D. Sinzinger, "Lattice Boltzmann methods for anisotropic diffusion of images", Mathematical Imaging, in review.
- [23] H. Karlsson and L. Svensson, "Feature Driven Compression for Curves by Curvature", Master's Thesis, Chalmers University of Technology, Sweden.
- [24] E. Comea, M. Comea, and B. Jawerth, "Hierarchical Shape Representation and Shape Preserving Approximations, *Wavelet Applications in Signal and Image Processing VI* (A. Laine, M. Unser and A. Aldroubi, eds.), Proceedings of SPIE, vol. 3458, pp.79-91, (1998).
- [25] J. Råde, V. Adolfsson, R. Andersson, and B. Johansson, "A Six Vertex Theorem for Polygons", to appear.
- [26] E. Cornea, R. Howard, and P.-G. Martinsson, "Solutions Near Singular Points to the Eikonal and Related First Order Non-linear Partial Differential Equations in Two Independent Variables," to appear in *Differential and Integral Equations Journal*.

#### D. LIST OF PARTICIPATING SCIENTIFIC PERSONNEL

Patrik Andersson
Alexander Andrianov
Colin Bennett
Emil Cornea
Fredrik Ekstedt
Fausto Espinal
Stephen Fenner
Michael Hilton
Ralph Howard
Terry Huntsberger
Björn Jawerth
Göran Kronquist

Toshiro Kubota Martin Lindberg Yiping Mao Per Gunnar Martinsson Johan Råde Henrik Storm Sundaram V. Weimin Zheng